

**Unit I****Calculus of Variations**

Introduction to variation problems - Euler's equation - Functional dependent on first and higher order derivatives - Functional dependent on functions of several independent variables - Some applications - Direct methods: Ritz methods.

**9 Hours****Unit II****Vector space**

Definition and examples of linear space - Linear dependence and independence - Basis and Dimension - Inner product space - Orthogonalisation process - Gram - Schmidt process Least - square problems - Applications of inner product spaces.

**9 Hours****Unit III****Eigen values and Eigen vectors**

Generalized Eigen values and Eigen vectors - Characteristic equation - Diagonalization - Eigen vectors & linear transformations - Complex eigen values - Applications to differential equations - Iterative estimates for Eigen values.

**9 Hours****Unit IV****Symmetric Matrices and Quadratic forms**

Diagonalization of symmetric matrices - Quadratic forms - Singular values decomposition - Change of basis.

**9 Hours****Unit V****Graph Theory**

Introduction - Basic terminology - Representation of graphs - Connected graphs - Matrix representation of graphs (excluding graphs) - Applications - Critical path method - Shortest path problems - Trees - Definition - Binary tree.

**9 Hours****Total:45+15 Hours****Reference(s):**

1. Elsgolts.L, *Differential Equation and Calculus of variations*, MIR Publishers, 1996.
2. David C Lay, *Linear Algebra and its Applications*, Pearson Education Asia, New Delhi, 2003.
3. Howard Anton, *Elementary Linear Algebra*, John Wiley & Sons, 2008.
4. Jonathan Gross and Jay Yellen, *Graph Theory and its Applications*, CRC Press, 2006.
5. Narsingh Deo, *Graph Theory with Applications to Engineering and Computer Science*, Prentice Hall, 2004.

**Unit I****Vector Spaces**

Vector spaces and subspaces – Linearly independent sets – Bases – Dimensions – Change of bases – Approximation to co-ordinate systems.

**9 Hours****Unit II****Linear Transformations**

System of linear equations – Row reduction and Echelon forms – Vector equations – The Matrix equation  $Ax = B$  – Solution sets of linear systems – Application of linear systems – Linear independence – Introduction to linear transformations – Matrix as linear transformation – Rank and Nullity – Linear equations.

**9 Hours****Unit III****Inner Product Spaces**

Inner product – Inner product spaces – Norm – Orthogonality – Gram-Schmidt orthogonalisation process – Orthogonal projections – Applications of inner product spaces.

**9 Hours****Unit IV****Eigen values and Eigen vectors**

Generalized Eigen values and Eigen vectors – Characteristic equation – Diagonalization – Eigen vectors and linear transformations – Complex Eigen values – Applications to differential equations – Iterative estimates for Eigenvalues.

**9 Hours****Unit V****Symmetric Matrices and Quadratic forms**

Diagonalization of symmetric matrices – Quadratic forms – Singular values decomposition – Applications to image processing.

**9 Hours****Total: 45 + 15 Hours****Reference(s)**

1. David C Lay, *Linear Algebra and its Applications*, Pearson Education Asia, New Delhi, 2003.
2. Seymour Lipschutz and Marc Lipson, *Schaum's Outline of Linear Algebra*, McGraw Hill Trade, New Delhi, Third Edition, 2000.
3. Howard A Anton, *Elementary Linear Algebra*, John Wiley & Sons, Singapore, Eight Editions, 2000.
4. Gilbert Strang, *Linear Algebra and its Applications*, Brooks/Cole Ltd, New Delhi, Third Edition, 2003

**Unit I****Fundamental Structures**

Set theory - Relationship between sets - Operations on sets - Set identities - Principle of inclusion and exclusion - Minsets. Relations: – Binary relations - Partial orderings - Equivalence relations. Functions: – Properties of functions - Composition of functions – Inverse functions.

12Hours

**Unit II****Logic**

Propositional logic – Logical connectives – Truth tables – Normal forms (conjunctive and disjunctive) - Predicate logic - Universal and existential quantifiers - Proof techniques – Direct and indirect – Proof by contradiction – Mathematical Induction.

12 Hours

**Unit III****Modeling Computation and Languages**

Finite state machines – Deterministic finite state machines (DFA) and Non-deterministic finite state machines (NFA) – Equivalence of DFA and NFA - Formal Languages – Classes of Grammars – Type 0-Context sensitive – Context free- Regular Grammar.

12 Hours

**Unit IV****Graph Theory**

Introduction to Graphs-Graph operations - Graph and Matrices – Graph Isomorphism – Connected Graphs – Euler Graphs - Hamilton paths and circuits – Shortest path problem.

12 Hours

**Unit V****Queue Models**

Characteristics of Queueing Models- Kendal's Notation - Single and Multi-Server Markovian queueing models – M/M/1, M/M/C (finite and infinite capacity) and (M/G/1) :( $\infty$ /GD) - Queueing applications.

12 Hours

Total: 60 Hours

**References:**

1. Kenneth H. Rosen "*Discrete Mathematics and its Applications*," Tata McGraw Hill Publications, New Delhi. 7th Edition, 2011.
2. Trembly J.P. and Manohar R., "*Discrete Mathematical Structures with Applications to Computer Science*", Tata McGraw Hill Publications Co. Ltd., New Delhi 2008.
3. Alan Doerr and Kenneth Levasseur, "*Applied Discrete Structures for Computer Science*," Galgotia Publications Pvt. Ltd. Delhi. 2010.
4. Ralph P Girmaldi and B.V. Ramana "*Discrete and Combinatorial Mathematics: An Applied Introduction*", Fifth Edition, Pearson Education Asia, Delhi, 2007.
5. H. A.Taha, *Operations Research - An Introduction*, 8th Edition, Prentice Hall of India Ltd, New Delhi, 2008.

**Unit I****Fundamental Structures**

Set theory - Relationships between sets - Operations on sets - Set identities - Principle of inclusion and exclusion - Minsets. Relations: – Binary relations - Partial orderings - Equivalence relations. Functions: – Properties of functions - Composition of functions – Inverse functions - Permutation functions. **9 Hours**

**Unit II****Logic**

Propositional logic – Logical connectives – Truth tables – Normal forms (conjunctive and disjunctive) - Predicate logic - Universal and existential quantifiers - Proof techniques – Direct and indirect – Proof by contradiction – Mathematical Induction. **9Hours**

**Unit III****Combinatorics**

Basics of counting – Counting arguments – Pigeonhole principle - Permutations and Combinations - Recursion and Recurrence relations – Generating functions. **9 Hours**

**Unit IV****Modeling Computation and Languages**

Finite state machines – Deterministic and Non- deterministic finite state machines – Turing Machines - Formal Languages – Classes of Grammars – Type\_0 – Context Sensitive – Context Free – Regular Grammars – Ambiguity. **9 Hours**

**Unit V****Finite State Automata**

Finite State Automata- Deterministic Finite State Automata (DFA), Non Deterministic Finite State Automata (NFA) – Equivalence of DFA and NFA – Equivalence of NFA and Regular Languages.

**9 Hours****Total: 45 +15 Hours****References:**

1. 1. Kenneth H. Rosen, *Discrete Mathematics and its Applications*, Tata McGraw Hill Publications, New Delhi. 7th Edition, 2011.
2. Trembly J.P. and Manohar R., *Discrete Mathematical Structures with Applications to Computer Science*, Tata McGraw Hill Publications Co. Ltd., New Delhi 2008..
3. Alan Doerr and Kenneth Levasseur, *Applied Discrete Structures for Computer Science*, Galgotia Publications Pvt. Ltd. Delhi. 2010.
4. Ralph P Girmaldi and B.V. Ramana, *Discrete and Combinatorial Mathematics: An Applied Introduction*, Fifth Edition, Pearson Education Asia, Delhi, 2007.
5. J.E. Hopcroft, R. Motwani and J.D. Ullman, *Introduction to Automata Theory, Languages and Computations*, Second Edition, Pearson Education, 2003.

**Unit I****Probability and Random Variables**

Probability concepts – Random Variables – Moment generating function – Standard distributions - Binomial - Poisson - Rectangular or Uniform – Normal - Exponential distributions - Functions of random variables - Two dimensional random variables.

**9 Hours****Unit II****Stochastic Processes**

Classification – Stationary and Random process – Markov process – Markov chains – Transition probability – Classification of Markov chain – Limiting distribution – First passage time – Poisson process – Birth and death process.

**9 Hours****Unit III****Queue Models**

Characteristics of Queueing Models- Kendal's Notation-Single and Multi-Server Markovian queueing models M/M/1, M/M/C (finite and infinite capacity) and ( M/G/1 ):( $\infty$ /GD) - Queueing applications.

**9 Hours****Unit IV****Simulation and Applications**

Introduction – Types of simulation – Limitations of simulation techniques – Phases of simulation study – Generation of random numbers – Monte Carlo simulation – Applications to queueing problems.

**9 Hours****Unit V****Classical Optimization Theory**

Unconstrained external problem – Newton Raphson method – Equality constraints – Lagrangian method – Kuhn Tucker conditions.

**9 Hours****Total: 45+15= 60 Hours****References**

1. Richard Johnson, *Miller and Freund's Probability and Statistics for Engineers*, Prentice Hall, New Delhi, 7<sup>th</sup> Edition, 2007.
2. S. D. Sharma, *Operations Research*, Kedar Nath, Ramnath & Co, Meerut, 2004.
3. S. C. Gupta and V. K. Kapoor, *Fundamentals of Mathematical Statistics*, Sultan Chand & Sons, 2001.
4. H. A. Taha, *Operations Research – An Introduction*, 8<sup>th</sup> Edition, Prentice Hall of India Ltd, New Delhi, 2008.

**Unit I****Basic Concepts in Graph Theory**

Graph-degree of a vertex- degree sequence- sub graphs- vertex induced sub graphs. Complement of a graph- self complementary graphs- walk- path- connectivity- eccentricity- radius-diameter- vertex and edge cuts- vertex partition- Independent set- clique.

**12 Hours****Unit II****Special Classes of Graphs**

Digraph- orientation, strongly, weakly and unilaterally connected digraphs- Directed acyclic graph. Adjacency matrix and incidence matrix of graphs. Trees- Spanning Trees- Matrix Tree theorem. Complete graphs-Bipartite graphs-Grid graphs.

**12 Hours****Unit III****Eulerian and Hamiltonian Graphs**

Eulerian graphs- Euler's theorem-Hamiltonian graphs- Bondy- Chvatal theorem- Traveling salesman problem. Planar graphs- Euler's formula-Kuratowski's theorem- Embedding and dual graphs.

**12Hours****Unit IV****Linear Programming**

Definition- Simplex-Two-phase simplex- Big M-method and Dual simplex algorithms.

**12 Hours****Unit V****Dynamic Programming**

Multistage decision process- Computational procedure-Final and Initial value problems- Continuous Dynamic programming- Discrete Dynamic programming.

**12 Hours****Total: 60 Hours****Reference(s)**

1. Yellen J and Gross J, *Graph Theory and its Applications*, Chapman & Hall, 2006.
2. Taha H. A, *Operations Research – An Introduction*, Eighth Edition , Prentice Hall of India Ltd, New Delhi, 2008.
3. Narsingh Deo, *Graph Theory with Applications to Engineering and Computer Science*. Prentice Hall, 2004.
4. West D.B, *Introduction to Graph Theory*, Pearson Education, 2007.
5. Kocay. W and Kreher D.L., *Graphs, Algorithms and Optimization*, Chapman & Hall, 2006.

**Unit I****Solution of System of Linear and Nonlinear Equations and Curve Fitting**

Solution of system of linear equations: Gauss Elimination Method, Choleski Method, Iterative Methods, Relaxation Method- System of Non-Linear Equations-: Newton Raphson Method- Least Square Approximation- Fitting of Non-Linear Curves By Least Squares.

**12 Hours****Unit II****Numerical Integration: Newton-Cotes Integration**

Numerical Integration : Trapezoidal rule, Simpson's rules, Gaussian quadrature, adaptive integration, cubic spline functions - Bezier curves and B-splines.

**12 Hours****Unit III****Boundary Value Problems and Characteristic Value Problems**

Introduction - Shooting method, solution through a set of equations, derivative boundary conditions, Rayleigh-Ritz method, characteristic value problems, solution using characteristic polynomial method, Jacobi method, power method and Inverse power method.

**12 Hours****Unit IV****Numerical Solutions of Stationary Partial Differential Equations**

Laplace's equation: Laplace's equations, representations as a difference equation, Iterative methods for Laplace's equations, Poisson equation, derivative boundary conditions, irregular and non-rectangular grids, Matrix patterns, ADI method, applications to two dimensional heat flow problems.

**12 Hours****Unit V****Parabolic and Hyperbolic Partial Differential Equations:**

Introduction-Crank-Nicholson method, explicit method, derivative boundary condition, stability and convergence criteria, Parabolic equations in two or more dimensions, applications to one dimensional heat flow problems- Hyperbolic Partial differential equations: Solving wave equation by finite differences, stability of numerical method, method of characteristics, Wave equation in two space dimensions

**12 Hours****Total: 60 Hours****Reference(s)**

1. Gerald C. F and Wheatley P. O, *Applied Numerical Analysis*, Pearson Education, 2003.
2. Rajasekaran S, *Numerical Methods in Science and Engineering – A Practical Approach*, Wheeler Publishing, 2005.
3. Faires J.D and Burden R, *Numerical Methods*, Brooks/Cole Publishing Company, 2006.
4. Chapra C.S and Canale P.R, *Numerical Methods for Engineers with Software and Programming Applications*, Tata McGraw Hill, 2004.



**Unit I****Advanced Matrix Theory**

Matrix norms - Jordan canonical form - Eigen values - Generalized eigenvectors - Some applications of Eigen value problems - Singular value decomposition - Pseudo inverse - Least square approximations - QR algorithm.

**12 Hours****Unit II****Calculus of Variations**

Introduction to calculus of variational problems - Euler's equation - Functional dependent on first and higher order derivatives - Functional dependent on functions of several independent variables -Some applications - Direct methods: Ritz and Kantorovich methods.

**12 Hours****Unit III****Fourier Series**

Euler's formula - Dirichlet's conditions - General Fourier series - Fourier series expansion to different types of wave forms - change of intervals - Harmonic Analysis.

**12 Hours****Unit IV****Fast Fourier Transform**

Discrete convolution - Periodic sequence and circular convolution - Linear convolution through circular convolution - Discrete Fourier series and discrete Fourier transform - Fast Fourier transform - Decimation in time algorithm - decimation in frequency algorithm - Inverse DFT.

**12 Hours****Unit V****Soft Computing Techniques.**

Genetic Algorithm - ANT colony Optimization - Particle Swam Optimization.

**12 Hours****Total: 60 Hours****Reference Books:**

1. Elsgoltis, *Differential equations and Calculus of Variations*, MIR publishers, Moscow, 1970.
2. Bronson.R, *Matrix Operations*, Schaum's outline series, McGraw Hill, Newyork, 1989.
3. Gupta.A.S, *Calculus of Variations with Applications* Prentice Hall of India, New Delhi,1999.
4. Sankara Roa, *Introduction to Partial Differential Equations*, Prentice Hall of India, New Delhi, 2004.
5. Ervin Kreyszig, *Advanced Engineering Mathematics*, 8<sup>th</sup> Edition, John Wiley & sons, 2006.
6. Jun Sun and Choi-Hang Lai, *Particle Swarm Optimisation: Classical and Quantum Perspectives*, CRC Press, Florida, 2012.

**Unit – I****Differentiation, integration and matrices**

First order and second order differential equations, functions - applications in Biological Sciences, Integrating factors and Bernoulli equations, Linear ODE's with constant coefficients: Numeric integration and differentiation - exposure to software packages like Matlab or Scilab: Basics: vectors, matrices, determinants; Matrix addition and multiplication.

**9 Hours****Unit – II****Curve fitting**

Curve Fitting –fitting a straight line and second degree curve, Correlation and Regression. fitting a non linear curve, Bivariate correlation - application to Biological Sciences.

**9 Hours****Unit –III****Design of Experiments**

Design of Experiments – One way, two way classifications – Randomized Block Designs-Latin Square Designs – biological samples

**9 Hours****Unit –IV**

Sampling distributions - Large samples and Small samples. Testing of Null hypothesis-Z test, t test and  $\chi^2$  test. Type I and Type II errors. Fisher's F Test. Goodness of fit.

**9 Hours****Unit-V**

Design of Experiments –One way, Two way classifications – Randomied Block Designs-Latin Square Designs.

**9 Hours****Total: 45 Hours****References:**

1. E. Kreyszig, Advanced engineering mathematics, 8th Edition, John Wiley Co., 1999.
2. W. E. Boyce and R. DiPrima, Elementary Differential Equations, 8<sup>th</sup> Edition, John Wiley Co., 2005.
3. W.L.Mc-Cabe, J.C.Smith and P.Harriot, *Unit Operations in Chemical Engineering*, 5<sup>th</sup> Edition, McGraw Hill Inc., New York, 1993.
4. R.A.Johnson, *Probability and Statistics for Engineers* 6<sup>th</sup> Edition. Prentice Hall Publication.
5. Merton R .Hubbard, *Statistical Quality control for the Food Industry*. Kluwer Academic/Plenum Publishers, 2003.